NUCLEAR RADIATION SHIELDING STUDIES Report No. 6







MONTE CARLO CALCULATION OF THE SPECTRUM OF GAMMA RADIATION FROM A COLLIMATED CO-60 SOURCE

By E. E. MORRIS AND A. B. CHILTON

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UNIVERSITY OF ILLINOIS
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Nuclear Radiation Shielding Studies

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A. B. Chilton
Principal Investigator

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SUMMARY

This report gives the results of a Monte Carlo calculation of the energy spectrum and angular distribution of gamma radiation emitted by a collimated cobalt-60 source. It is an extension of a previous report from the University of Illinois (K. Preiss, "Monte Carlo Calculation of Self Shielding by Encapsulated Gamma Ray Sources," Univ. of Ill. Rpt. NRSS-3, August 1966).

The program developed is flexible enough to give results for a wide variety of geometric situations of source container and collimator; however, the results of the specific calculation are for the particular one used by the University of Illinois in its shielding experimentation.

Minor simplifications in the precise geometry have been made for ease of programming, but such simplifications are not of a nature to change the results to any appreciable extent.

In the Monte Carlo calculation, the major simplification in technique involves the use of a fictitious interaction to facilitate the handling of some of the boundary problems. In essence, if this interaction is properly introduced, two media having tabulated attenuation coefficients which are slightly different can be made to have the same total interaction coefficient for the purpose of calculating path lengths, and the points of boundary crossing between these two media need not be calculated. (This technique seems to have been first mentioned by Woodcock et al., U.S. AEC Rpt. TID 4500, May 1965.)

The output data are given in terms of 13 energy groups, from 1.4 MeV down to 0.1 MeV, and 3 angle groups. The angle groups involve: first, a narrow cone in which all radiation passing through the collimator without interaction must be included; a somewhat wider cone which is established by a secondary collimator placed on top the first to minimize lip scatter problems; and the remainder which includes all lip scatter out to 90° from the axis of the collimator. The first angular group contains about 80% of the emergent photons and the other two groups contain about 10% each.

For the spectrum in the first angular interval, scattered photons constitute 16%. The low energy spectrum rises to a peak in the energy

interval 0.2 to 0.3 MeV. The peak results primarily from the fact that the single-scattering cutoff energies for both source energies lie in this interval. The spectrum results almost entirely from scatterings in the source and its capsule, with very little contribution from collimator scatterings.

The results are in qualitative agreement with previous calculations published by Cormack and Johns for a somewhat similar situation (British Journal of Radiology, 31, No. 369, 497, 1958). Agreement is also good with experimental measurements of Costrell on encapsulated sources (Health Physics, 8, 261, 1962), except at very low energies.

Modifications of the emergent spectrum by introduction of lead filter plates across the collimator are included.

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ACKNOWLEDGEMENT

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ABSTRACT

A Monte Carlo calculation of the energy spectrum emitted by a collimated, Co-60 source is reported. The collimator assumed is very similar to one currently being used in experimental shielding studies at the University of Illinois. Radiation emerging from the collimator is classified into 13 equal-length energy intervals between 0.1 and 1.4 MeV , and into 3 direction intervals for angles relative to the collimator axis between 0° and 90° . Comparisons are made with experimental and theoretical work reported by others.

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I, INTRODUCTION

This report gives the results of a Monte Carlo calculation of the energy spectrum and angular distribution of gamma radiation emitted by a collimated Co-60 source. It is an extension of earlier work reported by Preiss (1) for uncollimated, encapsulated sources.

Preiss cites several instances where discrepancies between theoretical calculations and corresponding experimental results have been traced to neglect of source spectrum degradation due to scattering either in the source material or in material near the source. The spectra in this report are to be used as input for calculations of gamma-ray penetration through ribbed slabs. The results of these calculations in turn will be compared with results of experimental studies of ribbed-slab shielding properties being conducted at the University of Illinois.

The collimated source for which the present calculation was made is shown in Figure 1. The source being used in the experimental work mentioned above differs from the collimated source in Figure 1 in that the experimental source capsule is held in place by a collar made of Firth Heavy Metal. This alloy consists of about 90% tungsten with the remaining 10% consisting of copper and nickel. In Figure 1, the collar is regarded as "black." The approximation thus made is not expected to have a significant influence on the usefulness of the calculated results.

The Monte Carlo calculation on which the data in this report are based is described in Section II. The mass attenuation coefficients used in the calculation are given in Appendix B along with a description of the procedure employed to evaluate interaction coefficients for cobalt. The computer program for the Monte Carlo calculation is described in Appendix C.

Some experimental measurements of spectra from collimated Co-60 sources have been reported. (2,3,4) Among these, one of the sources considered by Costrell (2) corresponds fairly closely to the collimated source in Figure 1. We compare with one of his spectra in Section III. Also in Section III, our results are compared with the Monte Carlo work of Preiss (1) and with a calculation by Cormack and Johns. (5)

Frequently, in order to reduce the importance of low energy scattered radiation relative to primary radiation, the source spectrum is filtered by placing a thin sheet of lead between the source and the target. In Appendix A, spectra which have been filtered in this way are presented for lead thicknesses of 1/8 and 1/4 inch.

II. DESCRIPTION OF THE CALCULATIONAL BASIS OF THE MONTE CARLO PROGRAM

The axis of the collimator was taken as the Z-axis of a cartesian coordinate system. Photon positions were then given in terms of rectangular coordinates and photon directions were specified by direction cosines relative to each of the coordinate axes.

The Co-60 was assumed to be uniformly distributed in the cobalt metal (Figure 1). At the beginning of the calculation, a finite set of source points which were assumed to represent the uniform distribution were selected. The selection was made by dividing the source region into a number of equal volume increments and picking a single source point in each increment. Because of cylindrical symmetry, the volume increments were chosen in the shape of annuli. They were defined by dividing the source region into a number of equal thickness layers all parallel to the plane z = 0, and then further dividing each layer into several concentric rings. The source point for a particular volume increment was selected so that it was located on the XZ-plane with x > 0, halfway between the top and bottom planes, and halfway between the inner and outer radii of the volume. As the calculation progressed, source points were then systematically selected from this predetermined list so that for each of the source energies 1.17 and 1.33 MeV, the same number of photon histories originated at each source point.

Initial photon directions were sampled randomly from an isotropic distribution.

The basic interaction considered in the calculation other than absorption was Compton scattering. Absorption was taken primarily as photoelectric; but for the short energy interval 1.022 to 1.33 MeV, the pair production interaction was also treated as absorptive.

In addition, we followed the procedure first reported by Woodcock, et al. (6) and subsequently used by Preiss, (1) of introducing a fictitious

interaction to facilitate the handling of some of the boundary problems. This procedure may be described as follows: Consider two media with an interface between them. Let μ_1 and μ_2 be the linear attenuation coefficients for medium 1 and medium 2 respectively. Further, suppose $\mu_2>\mu_1$. If a photon interacts in medium 2 and is not absorbed, then we sample a path length to the next interaction point using the equation,

$$s = -\frac{1}{\mu_2} \ln \rho ,$$

where s is the path length and ρ is a random number between 0 and 1. If the path carries the photon across the interface into medium 1, we write,

$$\mu_2 = (\mu_2 - \mu_1) + \mu_{a1} + \mu_{s1}$$
 ,

where

$$\mu_1 = \mu_{a1} + \mu_{s1}$$

and where μ_{a1} and μ_{s1} are the linear absorption and scattering coefficients for medium 1. Three possible interactions are then considered instead of the usual two. The first, with probability

$$\frac{\mu_2 - \mu_1}{\mu_2}$$
 ,

is a fictitious interaction in which there is no energy loss, no change of direction, and no apsorption. The second, with probability

is a Compton scattering interaction. The third, with probability

$$\frac{\mu_{al}}{\mu_2}$$
,

is a photoelectric absorption. The introduction of the fictitious interaction in medium 1 allows us to use the linear attenuation coefficient μ_2 for sampling path lengths in both medium 1 and medium 2. Thus, it is no longer necessary to compute the coordinates of the crossing point every time the photon crosses an interface or to check which of the various bounding surfaces has been crossed first.

In the present calculation, the above procedure was used in the source and capsule, and separately in the collimator. In the source

and capsule, cobalt was medium 2 and iron was medium 1. In the collimator, lead was medium 2 and iron was medium 1. (In principle, it would have been possible to base transport in the whole assembly on lead; however, this would have resulted in a very large number of fictitious interactions in the source and capsule, with attendant increase in computer time.)

The air column along the axis of the collimator was treated as a vacuum. Thus, when a photon entered this region, it was moved along its trajectory until it either re-entered the collimator wall or source capsule, or until it passed out the end of the collimator. For this reason, it was necessary to compute the coordinates of the crossing point when the photon crossed one of the surfaces bounding the air column.

The calculation of crossing point coordinates is very simple when the photon crosses a plane $z=z_b$. If the photon starts at the point (x_i, y_i, z_i) and moves along a path with direction cosines u_x, u_y , and u_z , then the distance s which the photon travels to reach the plane $z=z_b$ is,

$$s = \frac{z_b - z_i}{u_z} .$$

The coordinates of the crossing point are given by,

$$x = x_i + su_x,$$

$$y = y_i + su_y,$$

$$z = z_h.$$

The calculation of crossing point coordinates is more complicated if the photon leaves the point (x_i, y_i, z_i) and crosses a cylindrical boundary with radius r. If x and y are the x- and y- coordinates of the crossing point, then

$$r^2 = x^2 + y^2$$

But x and y are given in terms of x_i and y_i by the equation,

$$x = x_{i} + su_{x},$$

$$y = y_i + su_y$$
,

where s is the distance from the point (x_i, y_i, z_i) to the crossing point. Therefore, s must satisfy the equation,

$$r^{2} = (x_{1} + su_{x})^{2} + (y_{1} + su_{y})^{2}$$

$$= x_{1}^{2} + y_{1}^{2} + 2s(u_{x}x_{1} + u_{y}y_{1})$$

$$+ s^{2}(u_{x}^{2} + u_{y}^{2}).$$

Solving this equation, we find,

$$s = \frac{-(u_{x}x_{1} + u_{y}y_{1}) \pm \sqrt{(u_{x}x_{1} + u_{y}y_{1})^{2} + (u_{x}^{2} - u_{y}^{2})(r^{2} - x_{1}^{2} - y_{1}^{2})}}{(u_{x}^{2} + u_{y}^{2})}.$$

The sign of the square root must be chosen according to the rules:

$$u_{x}x_{i} + u_{y}y_{i} \ge 0, \quad r^{2} > x_{i}^{2} + y_{i}^{2} \quad \text{plus sign;}$$
 $u_{x}x_{i} + u_{y}y_{i} < 0, \quad r^{2} \ge x_{i}^{2} + y_{i}^{2} \quad \text{plus sign;}$
 $u_{x}x_{i} + u_{y}y_{i} < 0, \quad r^{2} < x_{i}^{2} + y_{i}^{2}, \quad \text{minus sign.}$

Once s has been calculated, the coordinates of the crossing point are,

$$x = x_{i} + u_{x}s$$

$$y = y_{i} + u_{y}s,$$

$$z = z_{i} + u_{z}s.$$

Photon histories were terminated under the following conditions:

(1) if a photon entered a black region; (2) if at a given interaction point a photoelectric interaction was selected. (3) if the photon energy dropped below 0.1 MeV in iron or cobalt, or below 0.2 MeV in lead; or (4) if the photon left the collimator.

When a photon emerged from the end of the collimator, either from the air column or from the surrounding iron and lead a score was recorded. The direction cosine $\mathbf{u}_{\mathbf{z}}$ of the emergent photon was classified into one of the intervals $0.996 \le \mathbf{u}_{\mathbf{z}} \le 1.0 + 0.961 \le \mathbf{u}_{\mathbf{z}} < 0.996$, or $0 \le \mathbf{u}_{\mathbf{z}} < 0.961$ and its energy E was classified into one of 13. 0.1^{-} MeV energy intervals between 0.1 and 1.4 MeV. The scoring procedure consisted of adding the statistical weight of the photon (always unity in the present calculation) to a rinning total for the appropriate energy angular interval.

The three angular groups defined above were of interest with respect to the University of Illinois 24-curie (nominal) experimental source. All uncollided photons which emerged without penetrating any part of the lip of the collimator had to have direction cosines $\mathbf{u}_{\mathbf{z}} > 0.996$, while photons which emerged with $\mathbf{u}_{\mathbf{z}} < 0.996$ had to penetrate some portion of the lip. For the experimental source, most of the photons which emerged with $\mathbf{u}_{\mathbf{z}} < 0.961$ had to penetrate an auxiliary lead collimator which was placed above the main collimator, as indicated in Figure 1.

III. RESULTS AND COMPARISON WITH OTHER WORK

The results of the calculation described in the preceding section are given in Table 1. The data are based on one million histories. This large number of histories was required because of the small angle of collimation and because of the fairly large number (39) of energy-angle groups used in the calculation. About 63 minutes on the IBM 7094 at the University of Illinois were required for the calculation.

An analytical calculation of the number of uncollided photons which one would expect to emerge from the collimator was made. Penetration of the lip of the collimator was neglected. Using the normalization of Table 1, the analytical calculation predicted 781 photons. From Table 1, we see that 948 photons emerge in the energy intervals 1.1 to 1.2 MeV and 1.3 to 1.4 MeV and the angular interval 0.966 \leq u $_{\rm Z}$ \leq 1.0 . These photons may be regarded as uncollided. (An approximate estimate of the number of scattered photons contributing to the abovementioned energy intervals appears to be between 10 and 20 .) This means that approximately 17% of all uncollided photons emerging from the collimator have penetrated some portion of the lip.

The spectrum of gamma radiation emerging from the collimator in the angular interval 0.996 \leq u $_{\rm Z}$ \leq 1.0 is shown in Figure 2. Scattered photons contribute 16% of the area under the histogram. The low energy spectrum rises to a peak in the energy interval 0.2 to 0.3 MeV . The peak results primarily from the fact that the single-scattering cutoff energies for both source energies lie in this interval. The spectrum decreases rapidly below 0.2 MeV because of the increasing importance of the photoelectric effect at low photon energies.

TABLE 1

Number of photons par 0.1 MeV per 500,000 disintegrations of Co-60. The standard deviation for an entry in the table can be estimated by computing the square root.

Angular Interval Energy Interval (MeV)	0.996 ≤ u _z ≤ 1.0	0.961 ≤ u _z < 0.996	0 ≤ u _z < 0.961
1 4 > D > 1 2	402	7	
$1.4 > E \ge 1.3$	493	7	0
$1.3 > E \ge 1.2$	3	18	1
$1.2 > E \ge 1.1$	455	31	8
$1.1 > E \ge 1.0$	13	36	26
$1.0 > E \ge 0.9$	6	17	19
$0.9 > E \ge 0.8$	11	8	25
$0.8 > E \ge 0.7$	14	4	19
$0.7 > E \ge 0.6$	12	9	14
$0.6 > E \ge 0.5$	19	8	14
$0.5 > E \ge 0.4$	22	3	14
$0.4 > E \ge 0.3$	30	1	11
$0.3 > E \ge 0.2$	36	5	4
$0.2 > E \ge 0.1$	16	5	3
Sum	1130	152	158

The spectrum in Figure 2 results almost entirely from scatterings in the source and capsule. This can be seen if we compare with one of the spectra computed by Preiss (1) for an uncollimated, encapsulated source. In Figure 3, Preiss's spectrum for his source B is compared with the spectrum in Figure 2. Preiss's source consisted of a cobalt metal disk inside a steel capsule. The cobalt disk had the same dimensions as the disk in Figure 1. The capsule had the same radial dimensions as the capsule in Figure 1, but its length was only 0.5 cm. Preiss's data were computed for $0.9 \le u_z \le 1.0$, but it seems reasonable to assume that the shape of the spectrum was practically constant over this range of directions, especially in view of the similarity of Preiss's results (1) for $0.9 \le u_z \le 1$ and $0 \le u_z \le 0.1$. The good agreement between our spectrum and Preiss's indicates that the spectrum in Figure 2 is affected predominantly by the top half-centimeter of the encapsulated source.

Costrell (2) has measured spectra for a variety of encapsulated, Co-60 sources, both collimated and uncollimated. In Figure 4, the measured spectrum for his collimated source E2,5H is compared with the spectrum presented in Figure 2. His collimator was made of lead, was about 18 inches long, and had a diameter varying from 1 3/16 inches at the source to 1 1/2 inches at the mouth. The source consisted of a disk of cobalt metal with thickness 0.25 cm and diameter 1.7 cm. It was clad in aluminum of thickness 0.05 cm. The source was placed in a capsule made of steel and tungsten. The thickness of the source capsule between the cobalt and the end of the collimator was 0.035 inches of steel. The E2.5H source was selected for comparison because this thickness was almost the same as the corresponding thickness for the capsule in Figure 1. Agreement between the experimental and calculated results is quite good except in the energy interval 0.1 to 0.2 MeV.

Figures 5 and 6 show spectra for radiation which emerges in the angular intervals $0.961 \le u_z < 0.996$ and $0 \le u_z < 0.961$. Almost all the radiation emitted in these angular intervals must scatter at least once from the walls of the collimator. (Uncollided photons may contribute as much as 13% of the histogram area in Figure 5.) For every 100 photons which emerge from the collimator uncollided, i.e.

in the energy intervals 1.1 to 1.2 MeV and 1.3 to 1.4 MeV and in the angular interval 0.996 \leq u $_{\rm Z}$ \leq 1.0 , about 16 photons are emitted in each of the direction intervals represented in Figures 5 and 6. It is interesting to note that most of these photons have energies greater than 0.5 MeV .

Cormack and Johns (5) have reported a single-scattering calculation of the spectrum of radiation scattered from the walls of a collimator. Their collimator was made of lead and had a tapered opening with a minimum radius of 3 cm near the source and a maximum radius of 8 1/4 cm at a distance of 60 cm from the source. They calculated the spectrum at a point on the axis of the collimator 80 cm from the source.

In Figure 7, we have summed the spectra presented in Figures 5 and 6 and normalized to one uncollided photon emerging from the collimator. The shaded portion of the histogram represents the contribution from the direction interval $0.961 \le u_Z < 0.996$. The curve is the spectrum calculated by Cormack and Johns. It rises to a maximum value of about 2.5 at an energy of 1.13 MeV and then cuts off sharply. In the Monte Carlo calculation, the sharp peak is smeared out over several energy intervals, largely because of use of a finite sized source and detector.

Because of considerable geometric differences, we expect at best only qualitative agreement between the results of Cormack and Johns and the results in this report. Consequently, the near equality between the area under the curve and the area of the shaded histogram is probably somewhat fortuitous. The largest angle which radiation directions could have with respect to the axis of the collimator and be included in the calculation of Cormack and Johns was about 22° . The largest angle which was included in the calculation of the shaded histogram was about 16° (\approx \cos^{-1} 0.961). Considering only these two angles, we might therefore expect the area under the curve to be greater than the area of the shaded histogram. On the other hand, the lead collimator scatters radiation less efficiently than the steel liner of the collimator in Figure 1. It thus appears that the larger angle of acceptance in the Cormack and Johns calculation is approximately compensated by the relatively poorer scattering characteristics of lead.

IV. CONCLUSION

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The data presented in this report show that roughly 17% of the photons which emerge with their initial energies from the collimator in Figure 1 have penetrated some portion of the lip of the collimator. This number could probably be reduced somewhat if the steel liner of the collimator were replaced by lead.

It was also observed that for every 100 photons which are emitted from the collimator without energy loss, approximately 32 photons are scattered by the collimator wall and emerge along directions which cannot "see" the source directly. Most of these photons have energies in excess of 0.5 MeV with the most probable energy being about 1 MeV. This result is in qualitative agreement with earlier calculations published by Cormack and Johns (5). These collimator-scattered photons were not observed in the experimental measurements of Costrell (2) mainly because of the geometrical arrangement in which his measurements were made.

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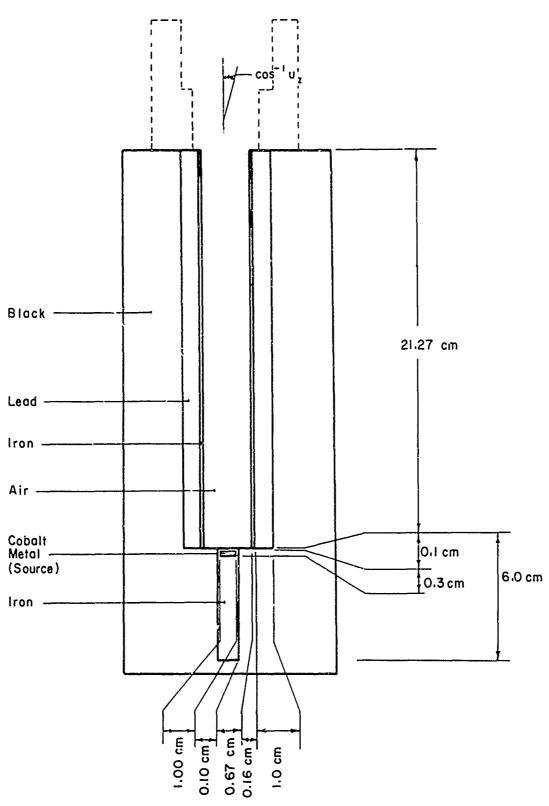


Figure 1. Source in collimator. The position of an auxiliary collimator which was placed on the main collimator when the experimental source was in use is indicated by the dashed lines at the top of the figure. The auxiliary collimator was not included in the computational model.

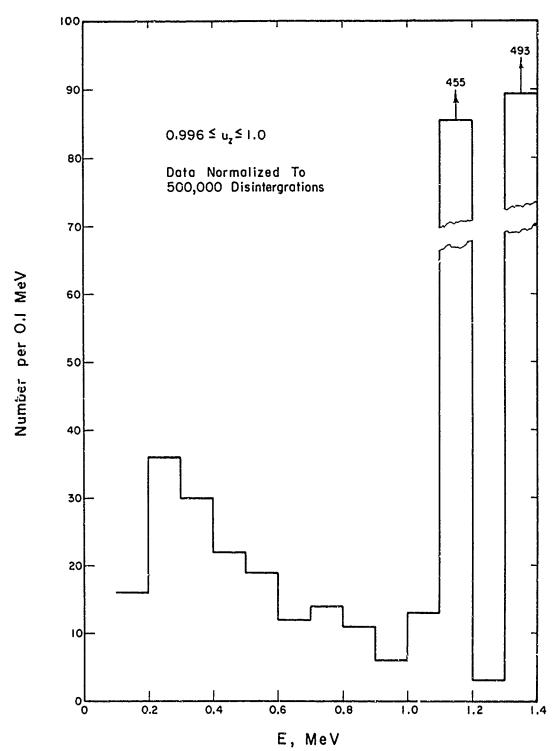


Figure 2. Spectrum of radiation emerging from the collimator in the direction interval 0.996 $\le u \le 1.0$. Photons in the energy intervals 1.1 to 1.2 MeV and 1.3 to 1.4 MeV are regarded as uncollided. If normalization to 1 curie is desired, multiply the given ordinates by 7.4 x 10^4 .

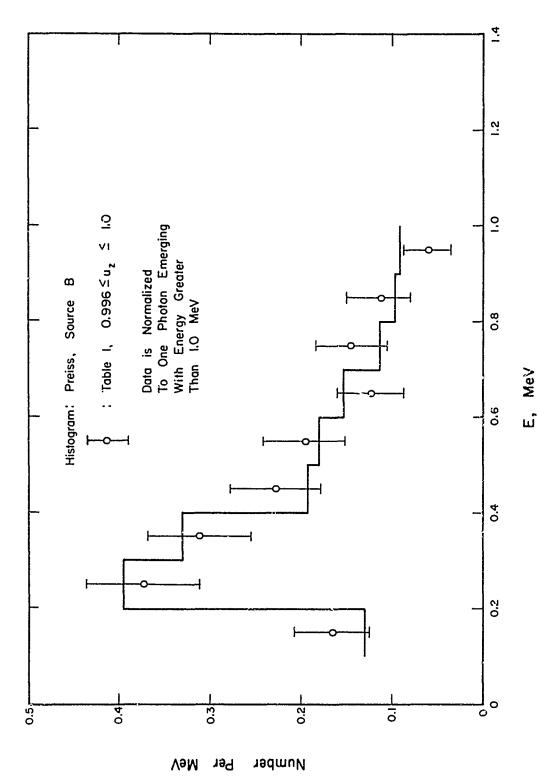


Figure 3. Comparison with spectrum calculated by Preiss for an uncollimated source. Error bars indicate standard deviation of our Monte Carlo results.

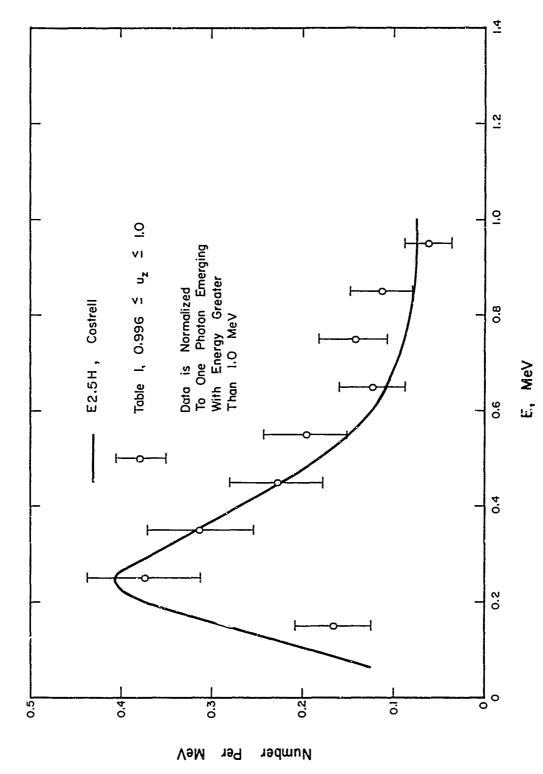


Figure 4. Comparison with spectrum measured by Costrell for a collimated source. Error bars indicate standard deviation of our Monte Carlo results.

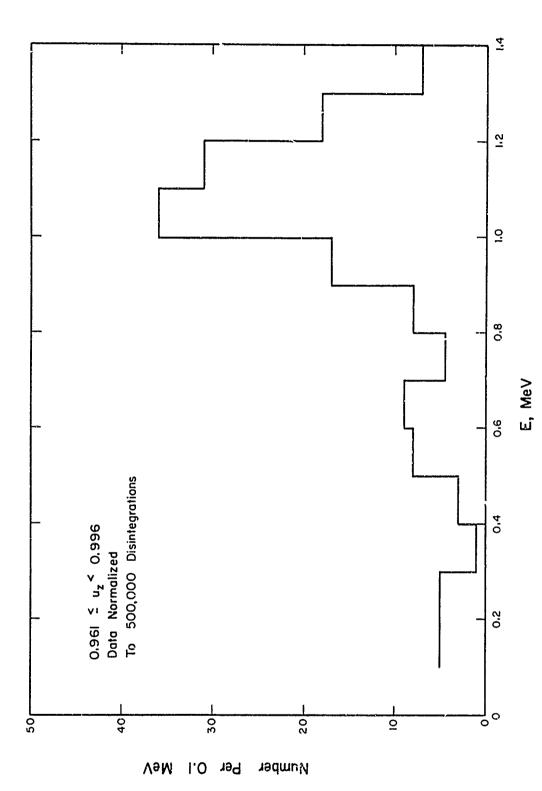
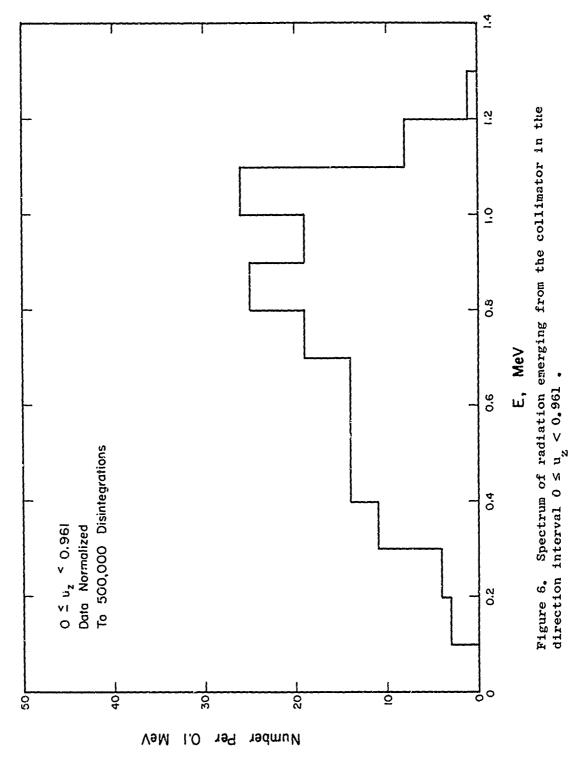


Figure 5. Spectrum of radiation emerging from the collimator in the direction interval 0.961 $\le u_z < 0.996$.



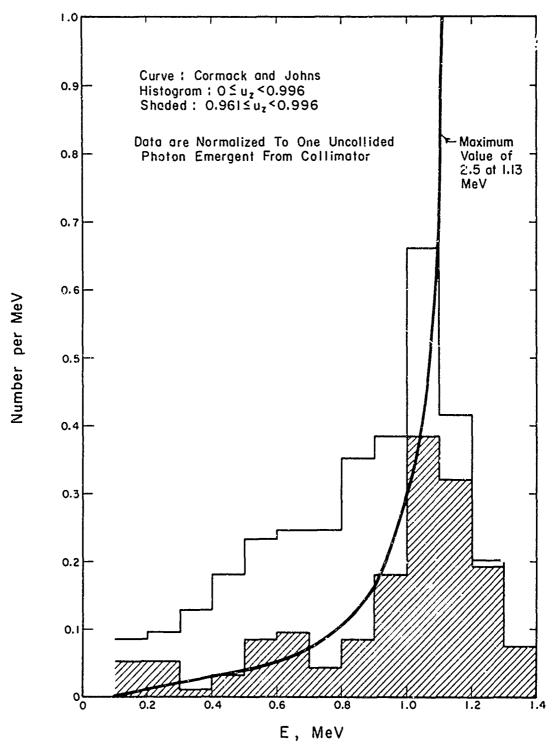


Figure 7. Comparison of present results with calculation by Cormack and Johns of the spectrum of radiation singly scattered from the walls of a collimator.

APPENDIX A

FILTERED SPECTRA

For use in experimental work at the University of Illinois, it was necessary to modify the collimator emergent spectrum of Figure 2 by assuming that radiation from the collimator subsequently passed perpendicularly through a thin lead sheet. A simple filtered spectrum was calculated in which scattering by the lead sheet was neglected. The results are given in Table Al. In the column for zero thickness, the spectrum was normalized to one photon with energy greater than 0.1 MeV . In the other columns, for a given energy interval, the number to the left of the slash was obtained by multiplying the corresponding number from the unfiltered spectrum by an exponential factor. The attenuation coefficient was evaluated at the mid-point energy of the interval. The number to the right of the slash resulted from renormalizing the filtered spectrum to one photon with energy greater than 0.1 MeV .

The spectra in Figures 2 and 5 were added together and filtered as described above for the spectrum in Figure 2. The resulting spectra for this case are presented in Table A2.

TABLE A1

Number of photons per 0.1 MeV for 0.996 $\leq u \leq$ 1.0 which are transmitted by lead sheets of different thicknesses.

Filter Thickness (inches) Energy Interval (MeV)	0	1/8	1/4
$1.4 > E \ge 1.3$	0.436	0.358/0.474	0.294/0.491
$1.3 > E \ge 1.2$	0.003	0.002/0.003	0.002/0.003
$1.2 > E \ge 1.1$	0.403	0.324/0.429	0.261/0.435
$1.1 > E \ge 1.0$	0.011	0.009/0.012	0.007/0.012
$1.0 > E \ge 0.9$	0.005	0.004/0.005	0.003/0.005
$0.9 > E \ge 0.8$	0.010	0.007/0.010	0.005/0.009
$0.8 > E \ge 0.7$	0.012	0.009/0.012	0.006/0.011
$0.7 > E \ge 0.6$	0.011	0.007/0.010	0.005/0.008
$0.6 > E \ge 0.5$	0.017	0.010/0.014	0.006/0.011
$0.5 > L \ge 0.4$	0.020	0.010/0.013	0.005/0.009
$0.4 > E \ge 0.3$	0.026	0.010/0.013	0.003/0.006
$0.3 > E \ge 0.2$	0.032	0.004/0.005	0.001/0.001
$0.2 > E \ge 0.1$	0.014	0	o

TABLE A2

Number of photons per 0.1 MeV for 0.961 $\leq u_{\rm Z} \leq 1.0$ which are transmitted by lead sheets of different thicknesses.

Filter Thickness (inches) Energy Interval (MeV)	0	1/8	1/4
1.4 > E ≥ 1.3	0.390	0.320/0.426	0.263/0.443
$1.3 > E \ge 1.2$	0.016	0.013/0.018	0.011/0.018
$1.2 > E \ge 1.1$	0.379	0.305/0.406	0.245/0.413
$1.1 > E \ge 1.0$	0.038	0.030/0.040	0.024/0.040
$1.0 > E \ge 0.9$	0.018	0.014/0.018	0.011/0.018
$0.9 > E \ge 0.8$	0.015	0.011/0.015	0.008/0.014
$0.8 > E \ge 0.7$	0.014	0.010/0.013	0,007/0,012
$0.7 > E \ge 0.6$	0.016	0.011/0.015	0.008/0.013
$0.6 > E \ge 0.5$	0.021	0.013/0.017	0.008/0.014
$0.5 > E \ge 0.4$	0.020	0.010/0.014	0.005/0.009
$0.4 > E \ge 0.3$	0.024	0.009/0.012	0.003/0.005
$0.3 > E \ge 0.2$	0.032	0.004/0.005	0.001/0.001
$0.2 > E \ge 0.1$	0.016	0	0
Total	1.00	0.750/1.00	0.594/1.00

APPENDIX B

MASS ATTENUATION COEFFICIENTS

The mass attenuation coefficient data used in the calculation are listed in Table Bl. The coefficients for iron and lead are from tabulations of Hubbell and Berger. (7) Since Hubbell and Berger did not include data for cobalt in their tabulations, data for this element were generated by a separate calculation as follows:

The total Compton interaction cross section was calculated using a tabulation of the Klein-Nishina formula. The cross sections for three other processes, viz., photoelectric effect, pair production in the field of the nucleus, and pair production in the field of an electron, were determined by an interpolation procedure using microscopic cross section data for iron and copper. Three primary steps were involved in the interpolation.

- A dominant functional dependence on the atomic number
 / was removed from the cross section data for iron
 and copper by division.
- 2. For fixed energy, a 'inear interpolation was performed on the data for iron and copper to get corresponding data for cobalt.
- 3. The cobalt data resulting from Step 2 were multiplied by the function of Z removed in Step 1.

The functional dependences assumed were $z^{4.5}$ for the photoelectric effect, z^2 for pair production in the field of the nucleus, and z^2 for pair production in the field of an electron.

TABLE B1 $\label{eq:mass_attenuation} \text{Mass Attenuation Coefficients } (\text{cm}^2/\text{g})^*$

Energy (MeV)	Iron	Cobalt	Lead
0.010	1.72.0	187.0	132.0
0.015	55.7	60.8	112.0
0.020	25.1	27.4	83.4
0,030	7.87	8,67	27.9
0.040	3.46	3.82	13.0
0.050	1.84	2.02	7.17
0.060	1.13	1.24	4.47
0.080	0.550	0.596	2.12
0.100	0.342	0.365	5.62
0,150	0.184	0.189	1.99
0.200	0.139	0.140	0.969
0.300	0.107	0.106	0.385
0.400	0.0921	0.0911	0,221
0.500	0.0829	0.0818	0.154
0.600	0.0761	0.0751	0.120
0.800	0.0664	0.0655	0.0856
1.000	0.0596	0.0587	0.0689
1.500	0.0486	0.0479	0.0509
2.000	0.0425	0.0419	0.0450
3.000	0.0361	0.0357	0.0415
4.000	0.0331	0.0328	0.0415
5.000	0.0315	0.0313	0.0424
6.000	0.0305	0.0304	0.0434
8.000	0.0299	0.0299	0.0460
10.000	0.0299	0.0300	0.0487

^{*} The densities assumed were $_3^{7.86}$ g/cm for iron, 8.71 g/cm for cobalt, and 11.43 g/cm for lead. The density for lead should have been 11.34 g/cm³. The influence of this mistake on the final results is expected to be negligible.

APPENDIX C

DESCRIPTION OF FORTRAN PROGRAM CØLLIMATØR

C.1 General Remarks

CØLLIMATØR performs a Monte Carlo calculation of gamma ray transport in a finite, multi-region medium having cylindrical symmetry. Boundaries of regions are defined by the walls of concentric cylinders and by planes passing through these cylinders perpendicular to their axis. A particular region is identified by a radial index NR and a vertical index NZ . A radial index NR indicates that the region is between concentric cylinders numbered NR and NR + 1 . The innermost cylinder is assigned the number two. Similarly, a vertical index NZ means that the region less between planes numbered NZ and NZ + 1 .

In addition, each region is assigned three other indexes: MAT, MAT2, and NSPL. MAT is object pseudo-material index. If it is positive, it identifies the material whose attenuation coefficient is to be used for simpling path lengths in the region (see Section II). If it is zero, the region is coid. The value of indicates that the region is black and the value of labels the region is a detector.

The index MAT2 i either positive or zero. It identifies the actual material in the region. If for a particular region its value is different from the value of MAT for the region, the fictitious interaction described in Section II is introduced as an alternative to photoelectric absorption or Compton scattering. MAT2 is assigned the value zero for detector regions, black regions, and voids.

The third index, NSPL, is a splitting parameter. Splitting was not used in the calculation for this report, but the program was written to allow for this possibility. If the NSPL value for a region is zero, then no splitting occurs in that region. If the value of NSPL is greater than zero, then upon interacting in the region, a photon is split into NSPL new photons. The statistical weight assigned to these new photons is the statistical weight of the original photon divided by NSPL. When a splitting occurs, the radial and vertical index of the region, the coordinates of the interaction point, the statistical weight, the photon

energy, and the direction cosines of the photon are stored. The history for each newly generated photon is then followed in turn until the histories of all the photons have been completed. A photon which results from a splitting may itself be split if it has a subsequent interaction in a region where NSPL is different from zero. A logic diagram for a CØLLIMATØR history with splitting included is shown in Figure C1. In the diagram, ISPL is an index which counts the number of interaction points where splitting has occured.

C.2 Description of Individual Subroutines

CØLLIMATØR (Main Program)

Subroutine called: LEARN, DATEX, TRACK, TEACH.

The program consists of a nest of five loops. The index NZSØ specifies the z coordinate of the source point, NRSØ the x coordinate of the source point is always zero), NESØ specified the source energy, and NSPE counts the number of histories completed for each source point, source energy combination. The product NSEG > NESX > NPSX > NZSX > LP is the total number of histories to be done.

Subroutine LEARN

Subroutine called: none.

All input data are read by this program. After the data have been read, they are immediately printed under headings which give either the variable name or a brief description of the variable.

The first card read contains 72 alphanumeric characters and when printed at the beginning of the calculation serves to identify the run. Input variables are listed and defined below in the order in which they occur in the subroutine.

NRAN: The number of random numbers to be rejected before starting the calculation.

NEAX: The number of energy intervals to be used in the calculation of spectra.

NTHX: The number of angular intervals to be used in calculating the directional distribution.

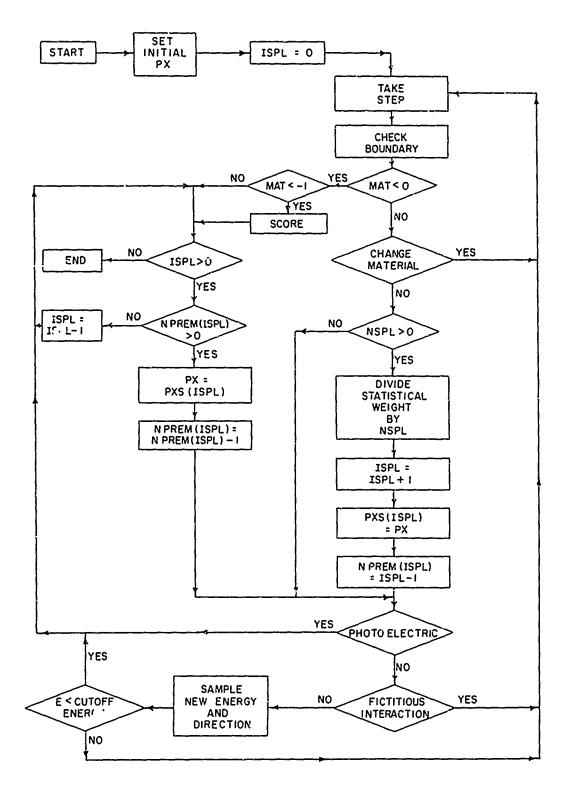


Figure Cl. Flow diagram of a CØLLIMATØR history. PX stands for photon energy, direc ion, statistical weight, vertical index, and radial index.

MXAX: The number of energies for which tabulated cross section data are to be read.

MATX: The number of materials in the collimator. In the present calculation, there were three; iron, cobalt, and lead.

NRAX: The number of radial boundaries.

NZAX: The number of horizontal boundaries.

NZTP: The index of the horizontal plane bounding the top of the collimator.

NRWL: The index of the radial boundary of the air column.

NZBT: The index of the horizontal plane bounding the bottom of the air column.

IHIX: This integer must be divisible by the product NESX * NRSX * NZSX.

LP: The product of LP and IKIX determines the number of histories to be done.

NESX: The number of source energies, Each source energy is regarded as equally likely.

NRSX: The number of x-coordinates for source points.

NZSX: The number of z-coordinates for source points. The number of source points is NZSX \star NRSX.

NR1: The radial index of the source region.

NZ1: The vertical index of the source region.

NASX: This index will be discussed later with the variable CTHØ and \$SØANG .

MAT,

MAT2: These variables were discussed in the general remarks at the beginning of this Appendix.

ESØ: A list of source energies.

ZH: A list of horizontal boundaries.

RHØ: A list of cylindrical boundaries. The first number in this list should be zero.

DEN: A list of densities for the materials in the collimator.

EB: A list of energies for which cross section data are to be read.

This list is read for each material but must be the same for each material.

XSECB: This is a list of interaction coefficients. If the indices specified for this variable are (M,1,NMAT), then we have the Compton interaction coefficient for the M'th energy, and the material with index NMAT. If the index 1 is replaced by 2, then we have the total attenuation coefficient. Note that if the densities were read in the order iron, cobalt, and lead, then the interaction coefficients must be read in the same order.

DUM1,

DUM2,

en en de la completa de la completa

DUM3,

DUM4: These are variables which are used to skip interaction coefficient data on the input cards which are not used in the calculation.

CTH: A list of lower limits for the intervals in which μ_Z is calssified for the directional distribution.

ECLS: A list of lower limits for the energy intervals used in the calculation of spectra.

NSPL: The splitting parameters were discussed in the general remarks at the beginning of this appendix. They should not be given the value one since this accomplishes the same thing as the value zero but increases the amount of bookkeeping required.

CTHØ, SØANG,

NASX: The program assumes that each source point emits radiation isotropically. However, it may be desirable to sample more photons in a certain range of directions and give them smaller weight while sampling fewer in other directions and giving them larger weight. These variables define a cumulative probability distribution at NASX values of the direction cosine relative to the z-axis. The probability distribution is assumed to be in histogram form. To sample all directions with equal probability, we read in the following table:

CTHØ	SØANG
-1	0.0
1	1.0

The values of SØANG must be in increasing order.

IWCT: For each material in the collimator, this variable lists the index of one of the energies in the list ECLS. We are thus able to specify different cutoff energies in different materials in the collimator.

Subroutine DATEX

Subroutines called: RAM2B, TABIN.

The tasks of this subroutine are listed below in the order in which they are done.

- 1. Rejects NRAN random numbers.
- 2. Re-arranges the tables of interaction coefficients so that the list EB is in descending order and multiplies the interaction coefficients for each material by the density. Since log-log interpolation is used, it takes logarithms of EB and XSECB.
- 3. Prepares an expanded table of interaction coefficients for 300 energies between zero and 1.5 MeV. The energy interval 0.005 MeV is used over the entire range. Hereafter, when an interaction coefficient is desired for an energy E, rather than interpolate, we compute an index using the formula NE = 200.0 * E + 0.5 and use the entry in these expanded tables corresponding to this index.
- 4. A table of sines and cosines is generated for 360 angles starting at 0.5° and proceeding in steps of 1° up to and including 359.5° . The sine and cosine for a random angle between 0° and 360° are then selected by computing an index according to the formula IPH = 360.0 * RAN, where RAN is a random number, and then choosing the sine and cosine in this table corresponding to the index IPH + 1.
- 5. A list RHØ2 of the squares of the radii of the cylindrical boundaries is generated.
- 6. Lists of source point coordinates RSØ and ZSØ are generated.
- 7. A list PART of floating point values of NSPL is generated.
- 8. Variables in which scores are accumulated, SPEC and SPEC2, are initially set equal to zero.
- The cutoff energy for each material is expressed in terms of its Compton wavelength.

Subroutine TRACK

Subroutines called: RAM2B, CHECK, VACUE, COMPT2, GRADE.

This subroutine performs the following tasks:

- 1. Source position, energy, and direction are selected to start a photon history. The energy of the photon is expressed in terms of the Compton wavelength.
- 2. Distances between interaction points are sampled.
- 3. The type of interaction is selected.
- 4. If splitting is used, the necessary bookkeeping is performed by this subroutine.

Subroutine CHECK

Subroutines called: none.

Without going into very much detail, we may outline the operation of the subroutine by the following steps:

- It checks to see if a horizontal boundary has been crossed.
 If it has, it then checks to see if a cylindrical boundary was crossed first.
- 2. If a horizontal boundary has not been crossed, it checks to see if a cylindrical boundary has been crossed. If not, it sets the index NSCT = 1 and returns to TRACK.
- 3. If a boundary is crossed, it compares the index MAT for the new region with MAT for the region where the photon started. If MAT is the same for both regions, then NR and NZ, the radial and vertical indices (see the general remarks at the beginning of this Appendix) are set equal to values appropriate to the new region. It then checks as in steps one and two to see if the photon actually stops in the new region or crosses into still another region. When a photon has stopped in a region, the subroutine sets NSCT = 1 and returns to TRACK.
- 4. If MAT for the region where the photon started and MAT for the new region are different, the coordinates of the crossing point are computed. It sets NSCT = 0 and returns to TRACK.
- If MAT for the new region is negative, the subroutine does not compute crossing point coordinates but immediately returns to TRACK.

Subroutine VACUØ

Subroutines called: none.

Control is transferred to this subroutine when the photon enters the air column. The coordinates of the point where the photon crossed into the air are given. The subroutine moves the photon along its current trajectory until the photon leaves the collimator or re-enters some part of the collimator. If the photon re-enters the collimator or source capsule, the coordinates of the re-entry point are computed.

Subroutine CØMPT2

Subroutine called: RAM2B.

This subroutine uses the method of Kahn (8) to sample a new photon direction and energy from the Klein-Nishina distribution.

Subroutine GRADE

Subroutines called: none.

When a photon enters a region designated as a detector, the subroutine adds the statistical weight of the photon to SPEC for the appropriate energy, angular interval. The squares of individual scores are cumulated in SPEC2.

Subroutine TEACH

Subroutine called: none.

This subroutine normalizes and prints the data. It also computes the fractional standard deviation of all results. In addition, the spectrum which is obtained by summing over all direction intervals and the directional distribution summed over all energy intervals are printed.

Liberal use is made of printed headings over all output data.

This makes the output fairly self-explanatory.

Subroutine TABIN

Subroutines called: none.

This subroutine performs a three-point interpolation simultaneously on each of MMAX functions of a single independent variable. XB is the list of independent variable values for which the functional values FB are given, and must be stored in descending order. NMAX is the number of values XB in the list and must be ≥ 3 . FX contains the list of functional values interpolated at X.

The index NTABIN must be unity the first time the subroutine is called. The subroutine then computes and stores certain differences and products which will be used over and over. Once this has been done, I.TABIN is set equal to two so that these differences need not be computed again on subsequent calls.

Functional Subroutine RAM2B

This function is used to generate a sequence of random numbers uniformly distributed between zero and one. It is written in machine language. The multiplicative congruential method is used. The multiplier is 5^{15} and the modulus is 2^{35} . The first number in the sequence is always $\left[5^{15}(2^{35}-1)\right]$ (mod 2^{35}). Thus, to change the initial random number, one rejects several random numbers before beginning the calculation.

C.3 Program Listings and Sample Output

Listings of the various FORTRAN programs are given on the following pages. The computer output for the calculation described in this report is reproduced following the listings.

```
FASTRAN
C
      COLLIMATOR
                                            4-20-67
       CALCULATES THE ENERGY-ANGLE SPECTRUM OF RADIATION EMERGING
С
      FROM A COLLIMATED SOURCE OF GAMMA RADIATION
      DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
      1
         MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
         NZREM(50), PART(10,10), RHO(10), RHO2(10), RSO(10), SPEC(20,30),
         SPEC2(20,30), SPH(360), UC(300,4), UT(300,4), UXREM(50),
         UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
         XSECB(25,2,4), YREM(50), ZH(10), ZREM(50), ZSO(10)
      DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
      COMMON CPH.CTH, DEN, EB, ECLS, ESO, IHIX, MAT, MAT2, MATX, MXAX,
         NE . NEAX . NEREM . NESO . NESX . NPREM . NR . NRI . NRAN . NRAX . NRREM . NRSO .
     2
         NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
        NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
         UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
         XSEC , XSECB , Y , YN , YREM , Z , ZH , ZN , ZREM , ZSO
      COMMON CTHO, IWCT, NASX, SOANG, LP
      CALL LEARN
      CALL DATEX
      L=0
    5 L=L+1
      NZSO= 0
   10 NZSO=NZSO+1
      NRSO# 0
   20 NRSO=NRSO+1
      NESO=0
   30 NESO=NESO+1
      NSPE=0
   40 NSPE=NSPE+1
      CALL TRACK
      IF (NSPE-NSEG) 40 + 50 + 50
   50 IF (NESO-NESX) 30,60,60
   60 IF(NRSO-NRSX)20,70,70
   70 IF (NZSO-NZSX) 10,80,80
   80 IF(L-LP)5,90,90
   90 CALL TEACH
      CALL SYSTEM
      END
       FASTRAN
Ç.
      SUBROUTINE LEARN
                                           4-20-67
C
      READS ALL INPUT DATA
      SUBROUTINE LEARN
      DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
        MAT2(10,10), NEREM(50), NPREM(50), NRREM(5C), NSPL(10,10),
        NZREM(50), PART(10,10), RHO(10), RHO2(10), RSO(10), SPEC(20,30),
        SPEC2(20,30), SPH(360), UC(300,4), UT(300,4), UXREM(50),
        UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
        XSECB(25,2,4),YREM(50),ZH(10),ZREM(50),ZSO(10)
      DIMENSION ESO(2) + CTHO(10) + SOANG(10) + IWCT(4) + WMAX(4)
      COMMON CPH+CTH+DEN+EB+ECLS+ESO+IHIX+MAT2+MAT2+MATX+MXAX+
        NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NRI, NRAN, NRAX, NRREM, NRSO,
     1
     2
        NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
       NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
```

```
UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
      XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
    COMMON CTHO, IWCT, NASX, SOANG, LP
    WOT6 . 10
 10 FORMAT(1HO)
    R1T7.20
    WOT6 . 20
20 FORMAT(72H
                                         )
    WOT6 + 10
    WOT6:30
30 FORMAT(72H
                                                                      NRWL
                NRAN NEAX NTHX MXAX MATX NRAX
                                                        NZAX
                                                              NZTP
   INZST
             IHIX LP)
    RIT7,45,NRAN,NEAX,NTHX,MXAX,MATX,NRAX,NZAX,NZTP,NRWL,NZBT,IHIX,LP
    WOT6,45, NRAN, NEAX, NTHX, MXAX, MATX, NRAX, NZAX, NZTP, NRWL, NZBT, IHIX, LP
 40 FORMAT(1216)
 45 FORMAT(1016,18,14)
    WOT6 . 10
    WOT6 , 50
50 FORMAT(36H NESX NRSX NZSX
                                                  NASX)
                                      NR1
                                             NZ1
    RIT7,40,NESX,NRSX,NZSX,NR1,NZ1,NASX
    WOT6 40 NESX NRSX NZSX NR1 NZ1 NASX
    WOT6:10
    WQT6 4 60
60 FORMAT(65H INDICES TO IDENTIFY PSEUDO-MATERIAL IN EACH REGION OF C
   1 OLL IMATOR)
    DO 70 NZ=1+NZAX
    RIT7,40, (MAT(NR,NZ),NR=1,NRAX)
    WOT6,40, (MAT(NR,NZ),NR=1,NRAX)
70 CONTINUE
    WOT6 + 10
    WOT6 , 80
80 FORMAT(58H INDICES TO IDENTIFY MATERIAL IN EACH REGION OF COLLIMAT
    DO 90 NZ=1+NZAX
    RIT7,40, (MAT2(NR,NZ), NR=1,NRAX)
    WOT6 + 40 + (MAT2 (NR + NZ) + NR=1 + NRAX)
90 CONTINUE
    WOT6 . 10
    WOT6,120
120 FORMAT(16H SOURCE ENERGIES:
    RIT7,130,(ESQ(NESO), NESO=1,NESX)
    WOT6 . 130 . (ESO(NESO) . NESO=1 . NESX)
130 FORMAT(10F7.3)
    WOT6 . 10
    WOT6 . 140
140 FORMAT(37H LOWER BOUNDARIES OF VERTICAL REGIONS)
    R1T7+150+(ZH(NZ)+NZ=1+NZAX)
    WOT6 , 150 , (ZH(NZ) , NZ=1 , NZAX)
150 FORMAT(9F8.2)
    WOT6 + 10
    WQT6+160
160 FORMAT (35H INNER BOUNDARIES OF RADIAL REGIONS)
    RIT7,150,(RHO(NR),NR=1,NRAX)
    WOT6 + 150 + (RHO(NR) + NR=1 + NRAX)
    WOT6 . 10
```

```
WCT6 + 170
170 FORMAT(17H DENSITIES, G/CM3)
    RIT7,180, (DEN(NMAT), NMAT=1, MATX)
    WOT6,180, (DEN(NMAT), NMAT=1, MATX)
180 FORMAT(1P6E11.3)
    WQT6 . 10
    DO 230 NMAT=1+MATX
    RIT7:190
    WQT6 + 190
190 FORMAT (72H
   1
    WQT6.200
200 FORMAT(24HOE'ERGY COMPTON
                                    TOTAL)
    DO 220 M=1.MXAX
    RIT7,210,EB(M),DUM1,XSECB(M,1,NMAT),DUM2,DUM3,DUM4,XSECB(M,2,NMAT)
    WQT6,210,EB(M),(XSECB(M,1,NMAT),1=1,2)
210 FORMAT(F7.3.1P7E10.3)
220 CONTINUE
    WOT6 . 10
230 CONTINUE
    WOT6 + 240
240 FORMAT(57H LOWER LIMITS ON COSINE THETA FOR ANGULAR CLASSIFICATION
    RIT7, 250, (CTH(NTH), NTH=1, NTHX)
    WOT6, 250, (CTH(NTH), NTH=1, NTHX)
250 FORMAT(8F9.5)
    WOT6 . 10
    WOT6 + 260
260 FORMAT(40H LOWER LIMITS FOR ENERGY CLASSIFICATIONS)
    RIT7,130, (ECLS(NEC), NEC=1, NEAX)
    WOT6,130,(ECLS(NEC),NEC=1,NEAX)
    WOT6:10
    WOT6 + 270
270 FORMAT(21H SPLITTING PARAMETERS)
    DO 280 NZ=1,NZAX
    RIT7,40, (NSPL (NR,NZ), NR=1,NRAX)
    WOT6, 40, (NSPL(NR, NZ), NR=1, NRAX)
280 CONTINUE
    WOT6 , 10
    WOT6 + 290
290 FORMAT(37H SOURCE SAMPLING ANGULAR DISTRIBUTION)
    RIT7, 250, (CTHO(NASO), NASO=1, NASX)
    WOT6, 250, (CTHO(NASO), NASO=1, NASX)
    RIT7.250, (SOANG(NASO), NASO=1.NASX)
    WOT6 . 250 . (SOANG (NASO) . NASO=1 . NASX)
    WOT6 . 10
    WOT6,300
300 FORMAT(22H ENERGY CUTOFF INDICES)
    RIT7,40,(IWCT(NMAT),NMAT=1,MATX)
    WOT6, 40, (IWCT(NMAT), NMAT=1, MATX)
    WOT6 . 10
    RETURN
    END
```

```
SUBROUTINE DATEX
C
                                           3-2-67
      EXPANDS INPUT DATA FOR TABLE LOOK-UP AND DOES OTHER PRELIMINARY
C
      WORK NEEDED FOR THE MAIN PART OF THE CALCULATION
      SUBROUTINE DATEX
      DIMENSION CPH(360) + CTH(20) + DEN(4) + EB(25) + ECLS(30) + MAT(10+10) +
        MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
        NZREM(50),PART(10,10),RHO(10),RHO2(10),RSO(10),SPEC(20,30),
     2
       SPEC2(20,30),SPH(360),UC(300,4),UT(300,4),UXREM(50),
        UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
     5 XSECB(25+2+4)+YREM(50)+ZH(10)+ZREM(50)+ZSO(10)
      DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
      COMMON CPH.CTH.DEN.EB.ECLS.ESO.IHIX.MAT.MATZ.MATX.MXAX.
        NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRKEM, NRSU,
        NRSX:NRWL, NSCT:NSEG:NSPL:NTHX:NZ:NZ1: NZAX:NZBT:NZREM:NZSO:
        NZSX+NZTP+PART+RAN+RHO+RHO2+RSO+S+SPEC+SPEC2+SPH+SUZ+UC+UT+
     3
         UX, CXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
        XSEC . XSECB . Y . YN , YREM . Z . ZH . ZN . ZREM . ZSO
      COMMON CTHO . IWCT . NASX . SOANG
      I=NIEATH
      DO 10 NRA=1 NRAN
   10 RAN=RAM2B(0)
      MXAX2=MXAX/2
      MM = M \times A \times + 1
      DO 15 M=1 MXAX2
      MM=MM-1
      DUM=EB(M)
      EB (M) = EB (MM)
      EB (MM) = DUM
      DO 15 I=1.2
      DO 15 NMAT=1 MATX
      DUM=XSECB (M. I. NMAT)
      XSECB(M.I.NMAT)=XSECB(MM.I.NMAT)
      XSECB (MM + [ + NMAT ) = DUM
   15 CONTINUE
      DO 30 M=1 + MXAX
      DO 20 1=1.2
      DO 20 NMAT=1.MATX
      XSECB(M, I, NMAT) = XSECB(M, I, NMAT) *DEN(NMAT)
   20 XSECB(M.I.NMAT)=ELOG(XSECB(M.I.NMAT))
   30 EB(M)=ELOG(EB(M))
      MATX2=2*MATX
      DO 50 NE=1 4300
      E=NE
      E=0.005*E
      E = ELOG(E)
      CALL TABIN(NTABIN. XSECB. EB. MXAX. MATX2. E. XSEC)
      DO 40 NMAT=1,MATX
      UC(NE + NMAT) = EXP(XSEC(1 + NMAT))
   40 UT(NE + NMAT) = EXP(XSEC(2 + NMAT))
   50 CONTINUE
      PH=-0.5
      DO 60 IPH=1.360
      PH=PH+1.0
      PHR=PH*0.017453293
      CPH(IPH) = COS(PHR)
```

60 SPH(IPH)=SIN(PHR)

```
DO 70 NR=1 , NRAX
 70 RH02(NR)=RH0(NR)**2
    NSPT # NRSX*NZSX
    NSPG= IHIX/NSPT
    IF (NSPG*NSPT-IHIX)80,110,80
 83 WOT6 + 90
 90 FORMAT(62HO NUMBER OF HISTORIES NOT DIVISIBLE BY NUMBER OF SOURCE
   1POINTS)
100 CALL SYSTEM
110 FNRSX=NRSX
    DO 120 NRSO=1+NRSX
    FNRS0=NRS0
120 RSO(NRSO)=0.5*(SQRT(((FNRSX-FNRSO)*RHO2(NR1)+FNRSO*RHO2(NR1+1))
      /FNRSX)+SQRT(((FNRSX-FNRSO+1.0)*RHO2(NR1)+(FNRSO-1.0)*RHO2(NR1
     +1))/FNRSX))
    FNZSX=NZSX
    DO 130 NZSO=1,NZSX
    FNZSO=NZSO
130 ZSO(NZSO)=((2.0*FNZSO-1.0)*ZH(NZ1+1)+(2.0*(FNZSX-FNZSO)+1.0)
     *ZH(NZ1))/(2.0*FNZSX)
    NSEG=NSPG/NESX
    IF (NSEG*NESX-NSPG) 140,160,140
140 WOT6 • 150
150 FORMAT(86H0 NUMBER OF HISTORIES FOR EACH SOURCE POINT NOT DIVISIBL
   1E BY NUMBER OF SOURCE ENERGIES)
    GO TO 100
160 DO 170 NR=1.NRAX
    DO 170 NZ=1, NZAX
170 PART(NR,NZ)=NSPL(NR,NZ)
    DO 180 NTH=1 NTHX
    DO 180 NEC=1 NEAX
    SPEC(NTH+NEC)=0.0
180 SPEC2(NTH, NEC) =0.0
    DO 190 NMAT=1+MATX
    NEC=IWCT(NMAT)
190 WMAX(NMAT)=0.511/ECLS(NEC)
    RETURN
    END
    FASTRAN
    SUBROUTINE TRACK
                                       3-13-67
    GENERATES PHOTON HISTORIES
    S' ROUTINE TRACK
   DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
      MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
      NZREM(50), PART(10,10), RHO(10), RHO2(10), RSO(10), SPEC(20,30),
      SPEC2(20,30), SPH(360), UC(300,4), UT(300,4), UXREM(50),
      UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
     XSECB(25,2,4),YREM(50),ZH(10),ZREM(50),ZSO(10)
   DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
   COMMON CPH, CTH, DEN, EB, ECLS, ESO, IHIX, MAT, MAT2, MATX, MXAX,
      NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRREM, NRSO,
     NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
     NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
      UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
```

С

C

```
XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
   CCMMON CTHO, IWCT, NASX, SOANG
   DIMENSION SUZREM(50)
   ISPL=0
   X=RSO(NRSO)
   Y=0.0
   Z=ZSO(NZSO)
   W=0.511/ESO(NESO)
   RAN=RAM2B(0)
   DO 2 NASO=2.NASX
   NA=NASO
   1F (RAN-SOANG (NASO)) 4,2,2
 2 CONTINUE
 4 RAN=RAM2B(0)
   DCTH=CTHO(NA)-CTHO(NA-1)
   UZ=CTHO(NA-1)+RAN*DCTH
   WT=DCTH/((SOANG(NA)-SOANG(NA-1))*2.0)
   RAN=RAM2B(0)
   IPH=360.0*RAN
   SUZ=SQRT(1.0-UZ**2)
   UX=SUZ*CPH(IPH+i)
   UY=SUZ*SPH(IPH+1)
   NR=NR1
   NZ=NZ1
   NE=102.2/W+0.5
10 NMAT=MAT(NR+NZ)
   RAN=RAM2B(0)
   NE=NE
   S=-ELOG(RAN)/UT(NE , NMAT)
   XN=UX*S+X
   YN=UY*S+Y
   ZN=UZ#S+Z
   CALL CHECK
   X=XN
   Y=YN
   Z=ZN
   NR=NR
   NZ≃I
   IF (MA .NR.NZ))80,27,30
20 CALL VACUO
   NR=NR
   NZ=NZ
   IF (MAT(NR,NZ))80,30,30
30 IF(NSCT)10:10:40
40 IF(NSPL(NR+NZ))60,60,50
50 ISPL=ISPL+1
   IF(ISPL-50)55,55,60
55 WT=WT/PART(NR.NZ)
   NPREM(ISPL) = NSPL(NR,NZ)-1
   XREM(ISPL)=X
   YREM(ISPL)=Y
   ZREM(ISPL)=Z
   UXREM(ISPL)=UX
   UYREM ( I SPL ) = UY
   UZREM(ISPL)=UZ
```

SUZREM(ISPL) =SUZ

WREM(ISPL)=W NEREM(ISPL)=NE

\$ C

```
WTREM(ISPL)=WT
    NRREM (ISPL) = NR
    NZREM (ISPL) = NZ
 60 NE=NE
    NMATHMAT (NR 1 NZ)
    NMATR=MAT2(NR + NZ)
    DIFAT=UT(NE, NMAT) -UT(NE, NMATR)
    DENOM = DIFAT+UC (NE + NMATR)
    RAN=RAM2B(0)
    IF (RAN-DENOM/UT(NE , NMAT)) 65 + 65 + 100
 65 RAN=RAM2B(0)
    IF (RAN-DIFAT/DENOM) 10,70,70
 70 CALL COMPT2
    NMAT=MAT2(NR+NZ)
    IF (W-WMAX(NMAT))10,100,100
 80 IF (MAT(NR,NZ)+1)90,100,100
90 CALL GRADE
100 [F([SPL)]40,140,110
110 [F(NPREM([SPL))120+120+130
120 ISPL=ISPL-1
    GO TO 100
130 NPREM(ISPL)=NPREM(ISPL)-1
    X=XREM(ISPL)
    Y=YREM(ISPL)
    Z=ZREM(ISPL)
    UX=UXREM(ISPL)
    UY=UYREM(ISPL)
    UZ ± UZREM ( [SPL )
    SUZ = SUZREM(ISPL)
    W# WREM ( I SPL )
    NE = NE REM (ISPL)
    WT=WTREM(ISPL)
    NR=NRREM ([SPL)
    NZ=NZREM(ISPL)
    GO TO 60
140 RETURN
    END
    FASTRAN
    SUBROUTINE CHECK
                                        3-2-67
    CHECKS TO SEE IF BOUNDARY HAS BEEN CROSSED
    SUBROUTINE CHECK
    DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
      MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
      NZREM(50), PART(10,10), RHO(10), RHO2(10), RSO(10), SPEC(20,30),
      SPEC2(20,30),SPH(360),UC(300,4),UT(300,4),UXREM(50),
      UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2:4),
      XSECB(25,2,4),YREM(50),ZH(10),ZREM(50),ZSO(10)
    DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
    COMMON CPH.CTH,DEN.EB,ECLS,ESO,IHIX,MAT,MAT2,MATX,MXAX,
      NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRREM, NRSO,
      NRSX,NRWL,NSCT,NSEG,NSPL,NTHX,NZ,NZ1, NZAX,NZBT,NZREM,NZSO,
      NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT:
```

```
UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
     XSEC , XSECB , Y , YN , YREM , Z , ZH , ZN , ZREM , ZSO
    COMMON CTHO. IWCT. NASX. SOANG
    DRAD=X*UX+Y*UY
    IF (DRAD) 20C + 10 + 10
10 IF(UZ)130,100,20
20 [F(ZN-ZH(NZ+1))100+30+30
30 SB=(ZH(NZ+1)-Z)/UZ
    X1 = SB * UX + X
    Y1=SB*UY+Y
40 IF(X1**2+Y1**2~RHO2(NR+1))90,70,50
50 NR=NR+1
    IF (MAT(NR+NZ)-MAT(NR-1,NZ))60,40,60
60 IF (MAT(NR, NZ)) 480,65,65
65 SUZ2=UX**2*UY**2
    SB=(SQRT(DRAD**2-SUZ2*(X**2+Y**2-RHO2(NR)))-DRAD)/SUZ2
    ZN=SB*UZ+Z
    XH=SS*UX+X
    YN#SB*UY+Y
    NSCT=0
    GO TO 480
 70 NR=NR+1
    NZ=NZ+1
    IF (MAT(NR,NZ)-MAT(NR-1,NZ-1))80,20,80
 80 IF (MAT(NR+NZ)) 480 +85 +85
 85 ZN=ZH(NZ)
    \times N = \times 1
    YN=Y1
    NSGT=0
    GO TO 480
 90 NZ=NZ+1
    IF (MAT(NR,NZ)-MAT(NR,NZ-1))80,20,80
100 IF(XN**2+YN**2-RHO2(NR+1))120,110,110
110 NR=NR+1
    JF (MAT(NR, NZ)-MAT(NR-1, NZ))60,100,60
120 NCCT=1
    CJ TO 480
130 IF(ZH(NZ)-ZN)100+140+140
140 SB=(ZH(NZ)-Z)/UZ
    X1=S6#UX+X
    Y1 = SB * UY+Y
150 IF(X1**2+Y1**2-RHO2(NR+1))190,170,160
160 NR=NR+1
    IF (MAT(NR+NZ)-MAT(NR-1,NZ))60,150,60
170 NR=NR+1
    NZ = NZ - 1
    IF (MAT(NR,NZ)-MAT(NR-1,NZ+1))180,130,180
180 IF (MAT(NR+NZ)) 480 + 185 + 185
185 ZN=ZH(NZ+1)
    XN=X1
    YN = Y1
    NSGT ± 0
    GO TO 480
190 NZ=NZ-1
    IF (MAT(NR+NZ)-MAT(NR+NZ+1))180+130+180
200 SUZ2=UX**2+UY**2
```

```
SM=-DRAD/SUZ2
    DS=S-SM
    IF(DS)220,220,210
210 XM=UX*SM+X
    YM=UY *SM+Y
    ZM=UZ*SM+Z
    GO TO 230
220 XM=XN
    YM=YN
    ZM=ZN
230 IF(UZ)390,340,240
240 IF (ZM-ZH(NZ+1))340,250,250
250 SB=(ZH(NZ+1)-Z)/UZ
    X1=SB*UX+X
    Y1=SB*UY+Y
260 IF(X1**2+Y1**2-RHO2(NR))320,290,270
270 NZ=NZ+1
    IF (MAT(NR, NZ) -MAT(NR, NZ-1))280,240,280
280 IF (MAT(NR+NZ)) 480 , 285, 285
285 ZN=ZH(NZ)
    XN = X1
    YN=Y1
    NSCT#0
    GO TO 480
290 NR=NR-1
    IF(NR)300,300,310
300 NR=NR+1
    GO TO 270
310 NZ=NZ+1
    IF (MAT(NR + NZ) - MAT(NR+1 + NZ-1))280 +240 +280
320 NR=NR-1
    IF (MAT(NR+NZ)-MAT(NR+1+NZ))330+260+330
330 IF (MAT (NR+NZ)) 480 + 335 + 335
335 SB=(-DRAD-SQRT(DRAD**2-SUZ2*(X**2+Y**2-RHO2(NR+1))))/SUZ2
    XN=SB*UX+X
    YN=SB*UY+Y
    ZN=SB*UZ+Z
    NSCT=0
    GO TO 480
340 IF(XM**2+YM**2-RHO2(NR))380,350,350
350 IF(DS)370,370,360
360 X=XM
    Y=YM
    Z=ZM
    DR AD = X*UX+Y*UY
    GO TO 10
370 XN=XM
    YN=YM
    ZN = ZM
    NSCT=1
    GO TO 480
380 NR=NR-1
    IF (MAT(NR+NZ)-MAT(NR+1+NZ))330+340+330
390 IF(ZH(NZ)-ZM)340,400,400
400 SB=(ZH(NZ)~Z)/UZ
```

X1=SB*UX+X

```
Y1=SB*UY+Y
 410 IF(X1**2+Y1**2-RHO2(NR))470,440,420
 420 NZ=NZ-1
      IF (MAT(NR+NZ)-MAT(NR+NZ+1))430,390,430
 430 IF (MAT(NR+NZ)) 480 +435 +435
  435 ZN=ZH(NZ+1)
      XN = X1
      YN = Y1
      NSCT=0
      GC TO 480
  440 NR=NR-1
      IF (NR) 450, 450, 460
  450 NR=NR+1
      GO TO 420
  460 NZ=NZ-1
      IF (MAT(NR+NZ)-MAT(NR+1,NZ+1))430,390,430
  470 NR=NR-1
      IF (MAT(NR+NZ)-MAT(NR+1+NZ))330+410+330
  480 RETURN
      END
       FASTRAN
      SUBROUTINE VACUO
C
                                          3-2-67
      MOVES PHOTON FROM POSITION IN HOLE TO WALL OR FLOCK OF COLLIMATOR
C
C
      OR TO DETECTOR
      SUBROUTINE VACUO
      DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECL5(30), MAT(10,10),
        MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
     1
        NZREM(50),PART(10,10),RHO(10),RHO2(10),RSO(10),SPEC(20,30),
     2
        SPEC2(20+30),SPH(360),UC(300,4),UT(300,4),UXREM(50),
        JYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
       XSECB(25+2+4), YREM(50), ZH(10), ZREM(50), ZSO(10)
      DIMENSION ESO(2) + CTHO(10) + SOANG(10) + IWCT(4) + WMAX(4)
      COMMON CPH.CTH.DEN.EB.ECLS.ESO.IHIX.MAT.MAT2.MATX.MXAX.
        NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRREM, NRSO,
        NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
        NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
        UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
        XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
      COMMON CTHO, IWCT, NASX, SOANG
      IF (UZ) 110,70,10
   10 SB=(ZH(NZTP)-Z)/UZ
      ZN=ZH(NZTP)
      XN±UX*SB+X
      YN=UY*SB+Y
      R2=XN**2+YN**2
      NZ#NZTP
      IF(R2-RHO2(NRWL))30,20,70
   20 NR=NRWL
      GO TO 120
   30 DO 40 NRC=1 + NRWL
      NR = NRC
      IF(R2-RH02(NRC))60,50,40
   40 CONTINUE
   50 [F(UX*XN+UY*YN)60:120:120
```

```
60 NR=NR-1
    GO TO 120
 70 NR=NRWL
    DRAD#UX*X+UY*Y
    SUZ2=UX**2+UY**2
    SB=(SQRT(DRAD**2-SUZ2*(X**2+Y**2-RH02(NRWL)))-DRAD)/SUZ2
    XN=UX*SB+X
    YN=UY*S8+Y
    ZN#UZ*SB+Z
    DO 80 NZC=NZBT+NZTP
    NZ±NZC
    IF(ZN-ZH(NZC))100,90,80
80 CONTINUE
90 IF(UZ)100,120,120
100 NZ = NZ - 1
    GO TO 120
110 SB=(ZH(NZBT)-Z)/UZ
    ZN=ZH(NZBT)
   XN=SB*UX+X
    YN#SB*UY+Y
    R2=XN**2+YN**2
   NZ=NZBT-1
    IF(R2-RH02(NRWL))30,20,70
120 X=XN
    Y=YN
    Z = ZN
    NSGT = 0
    RETURN
    END
    FASTRAN
    SUBROUTINE COMPT2
                                        3-2-67
    SAMPLE NEW DIRECTION AND ENERGY FROM COMPTON DISTRIBUTION
    SUBROUTINE COMPT2
    DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
      MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
     NZREM(50),PART(10,10),RHO(10),RHO2(10),RSO(10),SPEC(20,30),
     SPEC2(20,30),SPH(360),UC(300,4),UT(300,4),UXREM(50),
     UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
     XSECB(25,2,4),YREM(50),ZH(10),ZREM(50),ZSO(10)
   DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
    COMMON CPH+CTH+DEN+EB,ECLS+ESO+IHIX+MAT+MAT2+MATX+MXAX+
      NE + NEAX + NEREM + NESO + NESX + NPREM + NR + NR 1 + NRAN + NRAX + NRREM + NRSO +
      NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
     NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
      UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
      XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
    COMMON CTHO. IWCT. NASX, SOANG
10 RAN=RAM2B(0)
    IF (RAN-(1.0+T)/(9.0+T))20,20,30
20 RAN=RAM2B(0)
    R=1.0+RAN*T
   RAN=RAM2B(0)
    IF (RAN-4.0*(R-1.0)/(R*+2))40,40,10
```

```
30 RAN=RAM2B(0)
   R = (1 \cdot 0 + T) / (1 \cdot 0 + RAN + T)
   RAN=RAM28(0)
   IF(RAN-0.5*((W-R*W+1.0)**2+1.0/R))40,40,10
40 WN=W*R
   COM=1.0+W-WN
   W= WN
   NMAT=MAT2(NR+NZ)
   IF (W-WMAX(NMAT))45,80,80
45 SOM=SQRT(1.0-COM**2)
   NE=102.2/W+0.5
   RAN=RAM2B(0)
   IPH=360.0*RAN
   UZN=UZ*COM+SUZ*SOM*CPH(IPH+1)
   SUZN=SQRT(1.0-UZN**2)
   A#SUZ#SUZN
   IF (A-0.000001)50,50,60
50 UXN== CPH([PH+1] *SUZN
   UYN=SPH(JPH+1)*SUZN
   GO TO 70
60 CDPH= (COM-UZ*JZN)/A
   SDPH=SOM*SPH(IPH+1)/SUZN
   UXN=((UX*CDPH-UY*SDPH)*SUZN)/SUZ
   UYN=((UY*CDPH+UX*5DPH)*SUZN)/SUZ
70 UX≃UXN
   UY=UYN
   UZ¤UZN
   SUZ=SUZN
80 RETURN
   END
    FASTRAN
   SUBROUTINE GRADE
                                       3-2-67
   RECORDS SCORE WHEN PHOTON ENTERS DETECTOR
   SUBROUTINE GRADE
   DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
     MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
     NZREM(50) .PART(10,10) .RHO(10) .RHO2(10) .RSO(10) .SPEC(20,30) .
     SPEC2(20,30), SPH(360), UC(300,4), UT(300,4), UXREM(50),
     UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
     XSECB(25,2,4), YREM(50), ZH(10), ZREM(50), ZSO(10)
   DIMENSION E50(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
   COMMON CPH:CTH:DEN:EB:ECLS:ESO:IHIX:MAT:MAT2:MATX:MXAX:
     NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRREM, NRSO,
     NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZI, NZAX, NZBT, NZREM, NZSO,
    NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
     UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
     XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
   COMMON CTHO. IWCT. NASX. SOANG
   DO 10 NTH=1.NTHX
   HTNHHTL
   IF (UZ-CTH(NTH))10,20,20
10 CONTINUE
20 E=0.511/W
   DO 30 NEC=1 NEAX
```

NECL = NEC

IF (E-ECLS(NEC))30,40,40

ESPEC(NEC) = ESPEC(NEC)/HIX

```
30 CONTINUE
40 SPEC(JTH, NECL) = SPEC(JTH, NECL) + WT
   SPEC2(JTH, NECL) = SPEC2(JTH, NECL) + WT * * 2
   RETURN
   END
    FASTRAN
   SUBROUTINE TEACH
                                        4-20-67
   NORMALIZES AND PRINTS RESULTS
   SUBROUTINE TEACH
   DIMENSION CPH(360), CTH(20), DEN(4), EB(25), ECLS(30), MAT(10,10),
     MAT2(10,10), NEREM(50), NPREM(50), NRREM(50), NSPL(10,10),
     NZREM(50), PART(10,10), RHO(10), RHO2(10), RSO(10), SPEC(20,30),
     SPEC2(20,30), SPH(360), UC(300,4), UT(300,4), UXREM(50),
     UYREM(50), UZREM(50), WREM(50), WTREM(50), XREM(50), XSEC(2,4),
     XSECB(25,2,4),YREM(50),ZH(10),ZREM(50),ZSO(10)
   DIMENSION ESO(2), CTHO(10), SOANG(10), IWCT(4), WMAX(4)
   COMMON CPH, CTH, DEN, EB, ECLS, ESO, IHIX, MAT, MAT2, MATX, MXAX,
     NE, NEAX, NEREM, NESO, NESX, NPREM, NR, NR1, NRAN, NRAX, NRREM, NRSO,
     NRSX, NRWL, NSCT, NSEG, NSPL, NTHX, NZ, NZ1, NZAX, NZBT, NZREM, NZSO,
     NZSX,NZTP,PART,RAN,RHO,RHO2,RSO,S,SPEC,SPEC2,SPH,SUZ,UC,UT,
     UX, UXREM, UY, UYREM, UZ, UZREM, W, WMAX, WREM, WT, WTREM, X, XN, XREM,
     XSEC, XSECB, Y, YN, YREM, Z, ZH, ZN, ZREM, ZSO
   COMMON CTHO . IWCT . NASX . SOANG . LP
   DIMENSION ASPEC(20), ASPEC2(20), ESPEC(30), ESPEC2(30)
   WOT6 . 10
10 FORMAT(1HO)
   FLP#LP
   HIX=IHIX
   HIX=HIX*FLP
   DO 11 NEC=1.NEAX
   ESPEC(NEC)=0.0
   ESPEC2(NEC) = 0.0
   DO 11 NTH=1+NTHX
   ESPEC(NEC) = ESPEC(NEC) + SPEC(NTH + NEC)
11 ESPEC2(NEC) = ESPEC2(NEC) + SPEC2(NTH, NEC)
   DO 12 NTH=1 NTHX
   ASPEC(NTH)=0.0
   ASPEC2(NTH)=0.0
   DO 12 NEC=1 NEAX
   ASPEC(NTH) = ASPEC(NTH) + SPEC(NTH, NEC)
12 ASPEC2(NTH) = ASPEC2(NTH) + SPEC2(NTH + NEC)
   DO 15 NTH=1+NTHX
   ASPEC(NTH) = ASPEC(NTH)/HIX
   ASPEC2(NTH)=ASPEC2(NTH)/HIX
   ASPEC2(NTH) = (ASPEC2(NTH) - ASPEC(NTH) **2)/(HIX-1.0)
   IF (ASPEC (NTH)) 13, 14, 13
13 ASPEC2(NTH)=SQRT(ASPEC2(NTH))/ASPEC(NTH)
   GO TO 15
14 ASPEC2(NTH) =-10.0
15 CONTINUE
   DO 18 NEC=1+NEAX
```

```
ESPEC2(NEC) = ESPEC2(NEC) / HIX
   ESPEC2(NEC) = (ESPEC2(NEC) - ESPEC(NEC) **2) / (HIX-1.0)
    IF(ESPEC(NEC))16+17+16
16 ESPEC2(NEC) = SQRT(ESPEC2(NEC)) / ESPEC(NEC)
    GO TO 18
17 ESPEC2(NEC) =-10.0
18 CONTINUE
   DO 40 NTH=1.NTHX
   DO 40 NEC=1.NEAX
   SPEC(NTH+NEC) = SPEC(NTH+NEC)/HIX
    SPEC2(NTH, NEC) = SPEC2(NTH, NEC)/HIX
    SPEC2(NTH, NEC) = (SPEC2(NTH, NEC) - SPEC(NTH, NEC) **2)/(HIX-1.0)
    IF (SPEC(NTH, NEC))20,30,20
20 SPEC2(NTH, NEC) = SQRT(SPEC2(NTH, NEC))/SPEC(NTH, NEC)
    GO TO 40
30 SPEC2(NTH.NEC) =-10.0
40 CONTINUE
    WQ T6 . 50
50 FORMAT (46H ENERGY-ANGLE SPECTRA EMERGING FROM COLLIMATOR)
 60 FORMAT(65H CTH IS THE COSINE OF THE LARGEST ANGLE IN GIVEN ANGULAR
   ( INTERVAL)
    WQT6.70
 70 FORMAT (49H ECLS IS SMALLEST ENERGY IN GIVEN ENERGY INTERVAL)
 80 FORMAT(46H DATA ARE NORMALIZED TO ONE PHOTON FROM SOURCE)
    40T6 (10
    IF (NEAX-10)84,84,82
 82 NBOT=1
    NTOP=10
    GO TO 86
84 NBOT=1
    NTOP= NEAX
86 WOT6,90, (ECLS(NEC), NEC=NBCT, NTOP)
90 FORMAT(12H CTH, ECLS=F7.3,9F10.3)
    WOT6 + 10
    DO 110 NTH=1.NTHX
    WO76,100,CTH(NTH),(SPEC(NTH,NEC),NEC=NBOT,NTOP)
100 FORMAT(F7.3,1PE14.2,1P9E10.2)
110 CONTINUE
    WOT6 + 10
    WOT6, 111, (ESPEC(NEC), NEC=NBOT, NTOP)
111 FORMAT (7H SUM
                    1PE14.2,1P9E10.2)
    WQT5.10
    IF (NEAX-NTOP) 116 + 116 + 112
112 NBOT=NTOP+1
    NTOP=NTOP+10
    IF (NEAX-NTOP) 114 + 86 + 86
114 NTOP=NEAX
    GO TO 86
116 WOT6 120
120 FORMAT(59H FRACTIONAL STATISTICAL DEVIATION OF SPECTRA IN ABOVE TA
   1BLE)
    WOT6 . 10
    IF (NEAX-10) 124 . 124 . 122
```

122 NBOT=1

```
NTOP≈10
    GO TO 126
124 NBOT=1
    NTOP= NEAX
126 WOT6,90, (ECLS(NEC), NEC=NBOT, NTOP)
    WOT6 . 10
    DO 130 NTH=1.NTHX
    WOT6,140,CTH(NTH),(SPEC2(NTH,NEC),NEC=NBOT,NTOP)
130 CONTINUE
140 FORMAT(F7.3.F14.4.9F10.4)
    WQT6+10
    WQT6,141,(ESPEC2(NEC),NEC=NBOT,NTOP)
141 FORMAT(10H SUM DEV. F11.4.9F10.4)
    WOT6,10
    IF (NEAX-NTOP) 146, 146, 142
142 NBOT=NTOP+1
    NTOP=NTOP+10
    IF (NEAX-NTOP) 144 126 126
144 NTOP=NEAX
    GO TO 126
146 WOT6 + 150
150 FORMAT(30H
                      ANGULAR
                                    FRACTIONAL)
    WOT6 + 160
160 FORMAT(29H CTH DISTRIBUTION DEVIATION)
    DO 170 NTH=1.NTHX
    WOT6 . 180 , CTH(NTH) , ASPEC(NTH) , ASPEC2(NTH)
170 CONTINUE
180 FORMAT(F7.3,1PE12.2,0PF11.4)
    WOT6:10
    RETURN
   END
    FASTRAN
    SUBROUTINE TABIN
                                       28-8-64
    SUBROUTINE TABIN(NTABIN.FB.XB.NMAX.MMAX.X.FX)
    DIMENSION FB(25,8), XB(25), FX(8), XBAV(25), D1(25), D2(25)
    GO 10 (10,30), NTABIN
10 NMAX1=NMAX-1
    DO 20 N=2 . NMAX1
    XBAV(N) = (XB(N-1) + XB(N))/2.0
    D1(N) = (XB(N-1) - XB(N)) * (XB(N-1) - XB(N+)))
20 D2(N) = (XB(N) - XB(N-1)) * (XB(N) - XB(N+1))
   NTABIN=2
   NEXS=NMAX1-2
30 IF(X \sim XB(1))60.50.40
40 NX=2
    GO TO 200
50 NX=1
    GO TO 220
60 IF(X~XB(2))80,70,40
70 NX=2
    GO TO 220
80 [F(NEXS)90,110,140
90 WOT6 100
100 FORMAT (33HONOT ENOUGH BASE POINTS FOR TABIN)
```

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```
CALL SYSTEM
110 IF(X-XB(NMAX))130:120:130
120 NX=NMAX
    GO TO 220
130 NX=NMAX1
    GO TO 200
140 DO 170 N=3.NMAX1
    IF (X-XB(N))170+150+160
150 NX=N
    GO TO 220
160 NX=N
    GO TO 180
170 CONTINUE
    GO TO 110
180 IF(X-XBAV(NX))200,200,190
190 NX=NX-1
200 WT1 = (X - XB(NX)) * (X - XB(NX + 1)) / D1(NX)
    WT2=(X-XB(NX-1))*(X-XB(NX+1))/D2(NX)
    WT3=1.0-WT1-WT2
    DO 210 M=1+MMAX
210 FX(M) = WT1*FB(NX-1, M) + WT2*FB(NX, M) + WT3*FB(NX+1, M)
    RETURN
220 DO 230 M=1.MMAX
230 FX(M)=FB(NX,M)
    RETURN
```

END

COLLIMATOR RUN 23, COLLIMATED COBALT SOURCE, PRODUCTION, 4-24-67
NRAN NEAX NTHX HXAX HATX NRAX NZAX NZTP NRWL NZBT IHIX LP 1090 13 3 25 3 6 6 4 5 10000 100
NESX NRSX NZSX MIL NZI NASX 2 10 5 1 3 2
FY PSEU00-MATERI
2 -1 -1 -1 2 -1 -1 -1 2 -1 -1 -1
INDICES TU IDENTIFY MATERIAL IN EACH REGION OF COLLIMATOR
110000000000000000000000000000000000000
SOURCE EMERGIES 1.330 1.170
LOWER BOUNDARIES OF VERTICAL REGIONS -100.00 .00 5.60 5.90 6.00 27.27
INNER BOUNDARIES OF RADIAL REGIONS • 04 • 50 • 60 1.27 1.43 2.43
DENSITIES, G/CM3 7.860E 00 8.710E 00 1.143E 01
THE PARTY OF THE P

TOTAL	
.C10 1.7956-01 1.716E 02	
1.763E-01 5.569E	
1.732E-01 2.508E	
1.674E-01 7.875E	
1.621E-01 3.461E	
1.5746-01 1.8398	
1.5296-01	
1.450E-C1	
1.3816-01	
~	
.200 1.139E-01 1.391E-01	
•300 9.905E-02 1.066E-01	
.400 8.875E-02 9.208E-02	
8.103E-02	
.600 7.496E-02 7.612E-02	
6.584E-02	
5.919E-02	
4-808E-02	
4.102E-G2	
3.225E-02	
2.696E-02	
5.000 2.328E-02 3.146E-02	
6,000 2,058E-02 3,055E-02	
10.000 1.434E-02 2.989E-02	
COBALT, 2-21-67, MACROSCOPIC CROSS-SECTION, CM2/G	
ENFRGY COMPTON TOTAL	
1.767E-61 1	
1.735E-01 6.082E	
1.706E-01 2.737E	
1.648E-01 8.667E	
1.596E-C1 3.816E	
1.550E-01 2.025E	
1.5055-01	
1.4276-01	
1 - 3005 - 01	
• 120 1.2.24=101 1.893=-01 - 201 1.20=-01 1.404=-01	

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									•2/6) PROCESSED ON 2/4/67							,														
									FOR PB (UNIT=CM.																					
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- 1		1.000 5.828E-02		3.000 3.175E-02	- 1	~ ~	8-000 1-6586-02	,	MACORSCOPIC	ENERGY COMPTON	.010 1.5268-01	-	ヿ゙	.030 1.4246-01	1	.050 1.338E-01			~ (.300 8.424E-02				- 1	3.000 2.743E-02	- 1	5.000 1.981E-02 6.000 1.750E-02	1	- 1

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ENERGY CUTOFF INDICES	ES	į	į							
13 13 12										
BNERGY-ANGLE SPECIRA EMERGING FROM COLLIMATOR	A EMERGING	FROM COLLIM	ATOR							
CTH IS THE COSINE OF THE LARGEST ANGLE IN GIVEN ANGULAR ECLS IS SMALLEST ENERGY IN GIVEN ENERGY INTERVAL	JF THE LARGI	EST ANGLE IN	I GIVEN ANGU	ULAR INTERVAL	VAL					
DATA ARE NORMALIZED TO ONE PHOTON FROM SOURC) TO ONE PH	OTON FROM SO	URCE							
CTH, ECLS= 1.300	1.200	1.100	1.000	. 900	. 800	.700	. 600	.500	. 400	
		1	1.30E-05	1	1.106-05	1.40E-05	1.206-05	1.908-05	2.20E-05	
7	1	1	3.60E-05	- 1	8.00E-06	4-00E-C6	9.00E-06	8-30E-06	3.005-06	
.000 .00€ 00	00 1.00E-06	6 8.00E-06	2.6GE-05	1.90E-05	2.508-05	1.90E-65	1.40E-05	1.406-05	1.40E-05	
40-900-5	34 2-20F-05	5 4.548-04	7.508-05	4.20F-05	4.40F-05	3,705-65	3.50F-05	4.10F-05 3.90F-05	3.906-05	

				.460	. 2132 . 5773 . 2673	.1601				
				.500	.2294 .3536 .2673	.1562				
				099.	.2 <u>887</u> .3333 .2673	.1690				
		1		. 760	. 2673 . 5600 . 2294	.1644				
				935.	3536 2000	.1508				
			TABLE	006.	. 2425 . 2425 . 2294	.1543				
			IN ABOVE TABLE	1.000	. 2773 . 1667 . 1961	.1155				
.100	1.60E-05 5.30E-06 3.00E-06	2.40E-05	OF SPECTRA	1.100	.1796	.0450	.120	.2500	.2041	
. 200	3.605-05 1 5.00E-06 5	4.50E-05 2	DEVIATION	1.200	. 5773 . 2357 1.0000	.2132	. 200	. 1667 . 4472 . 5000	.1491	FRACTIONAL DEVIATION .0297 .0811
.360	3.00E-05 3 1.00E-06 5 1.10E-05 4	4.20E-05 4	STATISTICAL DEVIATION OF SPECTRA	1.300	.3780	-0447	•300	.1826 1.0000 .3015	.1543	1 1 1 1
CTH, ECLS=	996° 1 196° 1 1900°	4 HOS	FRACT! CNAL ST	CTH, ECLS*	996	SUH DEV.	CIH, ECLS=	. 996 . 961 . 200	SUM DEV.	ANGULAR CIH DISTRIBUTION -996 1.13E-03 -961 1.52E-24 -000 1.58E-04

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Collimator, gamma rays, radiation, radioisotope, shielding

A Monte Carlo calculation of the energy spectrum emitted by a collimated, Co-60 source is reported. The collimator assumed is very similar to one currently being used in experimental shielding studies at the University of Illinois. Radiation emerging from the collimator is classified into 13 equal-length energy intervals between 0.1 and 1.4 MeV, and into 3 direction intervals for angles relative to the collimator axis between 0° and 90°. Comparisons are made with experimental and theoretical work reported by others.

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